Psychological Methods

# Changing Dynamics: Time-Varying Autoregressive Models Using Generalized Additive Modeling

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In psychology, the use of intensive longitudinal data has steeply increased during the past decade. As a result, studying temporal dependencies in such data with autoregressive modeling is becoming common practice. However, standard autoregressive models are often suboptimal as they assume that parameters are time-invariant. This is problematic if changing dynamics (e.g., changes in the temporal dependency of a process) govern the time series. Often a change in the process, such as emotional well-being during therapy, is the very reason why it is interesting and important to study psychological dynamics. As a result, there is a need for an easily applicable method for studying such nonstationary processes that result from changing dynamics. In this article we present such a tool: the semiparametric TV-AR model. We show with a simulation study and an empirical application that the TV-AR model can approximate nonstationary processes well if there are at least 100 time points available and no unknown abrupt changes in the data. Notably, no prior knowledge of the processes that drive change in the dynamic structure is necessary. We conclude that the TV-AR model has significant potential for studying changing dynamics in psychology.

Keywords: time series, nonstationarity, autoregressive models, generalized additive models, splines

Supplemental materials: http://dx.doi.org/10.1037/met0000085.supp

Humans are complex dynamic systems, whose emotions, cognitions, and behaviors fluctuate constantly over time (Nesselroade & Ram, 2004; Wang, Hamaker, & Bergeman, 2012). In order to

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The research leading to the results reported in this paper was sponsored in part by Belgian Federal Science Policy within the framework of the Interuniversity Attraction Poles program (IAP/P7/06), as well as by Grant GOA/15/003 from the KU Leuven, and Grant G.0806.13 from the Fund of Scientific Research Flanders. We are thankful to Noémi Schuurman and Markus Eronen for their helpful comments on several versions of the article.

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study these within-person processes, and to determine how, why, and when individuals change over time, individuals need to be measured on a relatively large number of occasions (Bolger & Laurenceau, 2013; Ferrer & Nesselroade, 2003; Molenaar & Campbell, 2009; Nesselroade & Ram, 2004; Nesselroade & Molenaar, 2010), resulting in intensive longitudinal data that, if N = 1, are typically designated as time series (Walls & Schafer, 2006). Currently, a spectacular growth of studies gathering intensive longitudinal data is taking place (aan het Rot, Hogenelst, & Schoevers, 2012; Bolger, Davis, & Rafaeli, 2003; Mehl & Conner, 2012; Scollon, Prieto, & Diener, 2003). With this development, it has become possible to study dynamical processes of psychological phenomena in much greater detail than has hitherto been possible (Trull & Ebner-Priemer, 2013).

There are various aspects of within-person processes that one can choose to study in order to gather insights into psychological dynamics, of which *temporal dependence* is one particularly informative aspect (Boker, Molenaar, & Nesselroade, 2009; Hamaker, Ceulemans, Grasman, & Tuerlinckx, in press; McArdle, 2009). Temporal dependence concerns the degree to which current observations can be predicted by previous observations, for exam-

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ple, the degree to which an individual's emotional state at a given time point is predictive of her emotional state at subsequent time points (Jahng, Wood, & Trull, 2008; Kuppens, Allen, & Sheeber, 2010).

A popular approach to handling such temporal dependency is autoregressive (AR) modeling, a family of statistical models in which the structure of the time-dependency in the data is explicitly modeled through regression equations. Some autoregressive models are suited to study time dependence within a single individual (e.g., Hertzog & Nesselroade, 2003; Molenaar, 1985; Rosmalen, Wenting, Roest, de Jonge, & Bos, 2012; Stroe-Kunold et al., 2012), whereas multilevel techniques can model time dependence within multiple individuals simultaneously (e.g., Bringmann et al., 2013; de Haan-Rietdijk, Gottman, Bergeman, & Hamaker, 2014; Song, & Ferrer, 2012; Oravecz, Tuerlinckx, & Vandekerckhove, 2011). In addition, AR techniques can be applied in various frameworks, such as the Bayesian (e.g., Pole, West, & Harrison, 1994) and the structural equation modeling framework (SEM; e.g., Hamaker, Dolan, & Molenaar, 2003; McArdle, 2009; Voelkle, Oud, Davidov, & Schmidt, 2012).

A drawback of most AR models is that they are based on the assumption that the average value around which the process is fluctuating as well as the variance and the temporal dependency of the process are time-invariant. This is also known as the stationarity assumption (Chatfield, 2003). However, in the context of psychology this may not always be a realistic assumption. In fact, it could be argued that in many psychological time series studies a form of nonstationarity can be expected to be present (e.g., Bringmann, Lemmens, Huibers, Borsboom, & Tuerlinckx, 2014; Molenaar, De Gooijer, & Schmitz, 1992; Rosmalen et al., 2012; Tschacher & Ramseyer, 2009). Even more so, often the very reason why it is interesting and important to study dynamics of psychological processes lies in their nonstationary nature (Boker, Rotondo, Xu, & King, 2002; van de Leemput et al., 2014). For example, when an individual receives therapy, the aim is to accomplish change, such as a decrease in symptoms. Thus, instead of considering dynamics, such as temporal dependency, as static characteristics of an individual, it is more realistic to consider them as time-varying, which implies that standard AR models are unsuitable (Boker et al., 2002; Molenaar et al., 1992).

To overcome this limitation, time-varying AR (TV-AR) models have been developed (Dahlhaus, 1997). In these models, the parameters (the intercept and autoregressive parameter) of the AR model (most commonly an AR(1) model) are now allowed to vary over time, so the models can be applied to both stationary and nonstationary processes (Chow, Zu, Shifren, & Zhang, 2011). Most time-varying AR models used in psychology and econometrics are based on the state-space modeling framework (Chow et al., 2011; Koop, 2012; Molenaar, 1987; Molenaar & Newell, 2003; Molenaar, Sinclair, Rovine, Ram, & Corneal, 2009; Mumtaz & Surico, 2009; Prado, 2010; Tarvainen, Georgiadis, Ranta-aho, & Karjalainen, 2006; Tarvainen, Hiltunen, Ranta-aho, & Karjalainen, 2004; West, Prado, & Krystal, 1999). The state-space framework is very general and encompasses a wide variety of models, such as dynamic linear models. Hence, the framework is very powerful due to its generality, but the downside is that it requires learning (state-space) notation with which most psychologists are unfamiliar. In addition, state-space models require the user to specify the way parameters of the time-varying model vary over time (Belsley & Kuh, 1973; Tarvainen et al., 2004; for a notable exception see Molenaar et al., 2009), but in practice the required theories about the nature of the change are often lacking (Tan, Shiyko, Li, Li, & Dierker, 2012), or must be handled via explicit incorporation of spline-based or other nonparametric functions into a (confirmatory) state-space framework (Tarvainen et al., 2006). Doing so may entail high computational demands when the dimension of the unknown change forms to be explored is high. Thus, there is a clear need for a time-varying AR method that functions without prespecification and moreover is easy to apply for researchers in psychology.

As we will show in this article, one solution is to implement TV-AR models based on semiparametric statistical modeling using a well-studied elegant and easily applicable generalized additive modeling (GAM) framework (Hastie & Tibshirani, 1990; McKeown & Sneddon, 2014; Sullivan, Shadish, & Steiner, 2015; Wood, 2006). The crucial advantage of semiparametric TV-AR models in general is that they are data-driven, and thus the shape of change need not be specified beforehand (Dahlhaus, 1997; Fan & Yao, 2003; Giraitis, Kapetanios, & Yates, 2014; Härdle, Lütkepohl, & Chen, 1997; Kitagawa & Gersch, 1985). Furthermore, no state-space notation is needed, because the TV-AR model is closely related to and can be specified and estimated within the familiar regression framework. Software for applying the GAM framework is freely available in the mgcv package for the statistical software R (Wood, 2006). The package has well-functioning default settings, making it very user friendly.<sup>1</sup> By showing how the Fn1 TV-AR model can be applied with existing and easy to use software, we hope to make the TV-AR method accessible for a broad audience of psychological researchers.

The structure of the article is as follows. In the first section, a detailed explanation of the standard time-invariant AR is given. In the second section, we describe the general structure of the TV-AR model, and in the third section we explain in detail how the time-varying parameters are estimated, and also introduce the mgcv package in R, with which the TV-AR is estimated (McKeown & Sneddon, 2014; Wood, 2006). In the fourth section, we provide a simulation study and give guidelines on how to use the TV-AR model with the mgcv package. In the fifth section, we give an example from emotion dynamics research to illustrate the TV-AR method by applying it to two different subjects whose affect was measured over circa 500 days in the context of an isolation study, the MARS500 project (Basner et al., 2013; Tafforin, 2013; Vigo et al., 2013; Wang et al., 2014). This section is followed by concluding remarks and the Appendix with a description of the R-code used throughout the article. Additional details of the simulation study can be found in the online supplemental material.

#### Standard Time-Invariant AR

In this section, the standard time-invariant autoregressive (AR) model is explained in more detail. Code for the equations and

<sup>&</sup>lt;sup>1</sup> Note that a time-varying effect model that also allows fitting a semiparametric TV-AR model has recently been developed in SAS (Tan et al., 2012). However, it is less general and has fewer options for fitting a TV-AR model (e.g., at the moment it is only suitable for normally distributed time-varying models).

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figures in this section can be found in the *R-code* in the Appendix **AQ:1** under the heading II. Standard Time-Invariant AR.

Time series data consist of repeated measurements on one or more variable(s) taken from the same system (e.g., an individual, dyad, family, or organization). Typically, such data are statistically dependent, since all measures are taken from the same participant (e.g., answers on a questionnaire are likely to be related over time, Brandt & Williams, 2007; Velicer & Fava, 2003). This statistical dependence or autocorrelation that occurs in repeated measurement data is a central aspect that has to be accounted for when studying the underlying process. Furthermore, when this autocorrelation is not taken into account invalid estimates can occur.

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In psychology, the standard model used to deal with this statistical dependency is a Gaussian discrete time AR model.<sup>2</sup> An AR model accounts for the statistical dependency by modeling it explicitly, or in other words, the time series is regressed on itself (Hamaker & Dolan, 2009). The most basic form is an AR model of lag order 1 or AR(1):

$$y_t = \beta_0 + \beta_1 y_{t-1} + \varepsilon_t. \tag{1}$$

This amounts to a linear regression model with an intercept  $\beta_0$ , and the autoregressive coefficient  $\beta_1$ , representing the degree and direction of the relation between a measurement at a previous (lagged) time point (t - 1) and current time point (t) of a single variable y (Velicer & Fava, 2003) and can be estimated with ordinary least squares (OLS). The part of observation  $y_t$  that cannot be explained by the previous observation  $y_{t-1}$  is referred to as the innovation  $\varepsilon_t$  (Chatfield, 2003). Other terms for the innovation are random shock, perturbation, or dynamic error.<sup>3</sup> The innovations are assumed to be normally distributed with a mean of zero and variance  $\sigma_{\varepsilon}^2$  (Hamilton, 1994).

The autoregressive coefficient  $\beta_1$  can also be interpreted as the extent to which a current observation is predictable by the preceding observation (Hamaker & Dolan, 2009). A positive relationship indicates that high values of a variable (e.g., positive affect [PA]) at one time point are likely to be followed by high values in the next time period (see left panel of Figure 1). In contrast, a negative relationship would predict the opposite, namely low values of the variable during the next time period (Chatfield, 2003; Velicer & Fava, 2003), which typically results in a jigsaw pattern (see right panel of Figure 1).

An important assumption for an AR(1) model is stationarity. A distinction is made between strictly stationary and covariancestationary (also known as weakly or second-order stationary) processes. If a process is strictly stationary, the distribution of  $y_t$  and all joint distributions of y random variables are the same at all time points, and are thus time-invariant. Covariance-stationarity is a less strong assumption, as in this case only the first two moments of a distribution, the mean and the variance, and thus the parameters  $\beta_0$  and  $\beta_1$ , have to be time-invariant.<sup>4</sup> Furthermore, stationarity also requires that the autoregressive coefficient must lie between -1 and 1 (boundaries not included). In this case, the mean  $\mu$  and variance  $\sigma^2$  of the process in Equation 1 can be expressed as

$$\mu = \frac{\beta_0}{1 - \beta_1} \tag{2}$$

$$\sigma^2 = \frac{\sigma_{\varepsilon}^2}{1 - \beta_1^2}, \qquad (3)$$

showing that both are time-invariant (Chatfield, 2003; Hamilton, 1994).

Figure 1 shows two examples of a stationary process. Although the process fluctuates (changes) in both the left and right panel, the intercept, mean, autocorrelation and variance do not change over time. In an AR model, the intercept term  $\beta_0$  only has a substantial interpretation if a score of 0 is a possible value in the sample.<sup>5</sup> Fn5 Therefore, we prefer to work with the mean  $\mu$ , which can be interpreted as the value around which the process fluctuates.

# **Time-Varying AR**

Psychological data are often nonstationary, rendering a standard AR model inapplicable. In this section, we will therefore describe an alternative model, the TV-AR model, which can model nonstationarity. First, we will discuss nonstationarity, illustrated by two simulated examples with 150 time points (representing here the evolution of valence within an individual). Second, we will give a general overview of the TV-AR model. Information on statistical inference for the TV-AR model will be given in the next section. The code to make the figure in this section can be found in the *R*-code in the Appendix under the heading III. Time-Varying AR.

There are several sources that can give rise to a nonstationary process in which the intercept, mean, autocorrelation and (or) variance change over time. In psychological research, the focus has mainly been on detecting a type of nonstationarity that is due to a (gradual) change in the mean of a process, which is visible as a trend in the data. Consider for example the left panel of Figure 2, in which a simulated process of hypothetical valence scores for F2 an individual is shown. Here the autoregressive parameter does not change over time ( $\beta_1 = 0.2$ ), but the intercept does, as represented by the dashed line, and therefore the mean also changes. Thus, a trend in the data is present.

To deal with a trend, common approaches in psychology have been *detrending* and *modeling the trend*. In the first method, data are made stationary by subtracting the values of a fitted trend from

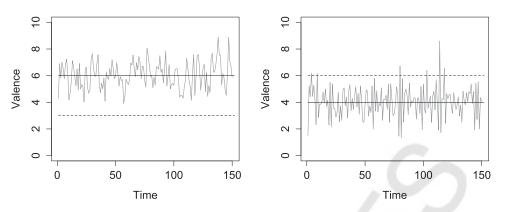
<sup>&</sup>lt;sup>2</sup> In discrete time AR models the measurements of the process are assumed to be equally spaced, meaning that the distance between the measurements is the same through the whole study. If time points were not equally spaced, the autoregressive coefficient would have a different meaning across occasions. This is in contrast to continuous time AR models, where the intervals between time points do not have to be equal (see for more information: Bisconti, Bergeman, & Boker, 2004; Deboeck, 2013; Oravecz et al., 2011; Voelkle & Oud, 2013; Voelkle et al., 2012).

<sup>&</sup>lt;sup>3</sup> The term dynamic error is used to pit this error against the well-known measurement error. The difference between the two error terms is that while measurement error is occasion-specific, affecting the scores only at a single occasion, dynamic error tends to affect subsequent occasions as well due to the underlying temporal dependency in the process (Schuurman et al., 2015). In the current study we restrict our focus to processes without measurement error.

<sup>&</sup>lt;sup>4</sup> As we study normally distributed processes here, it is interesting to note that in this case covariance-stationarity implies strict stationarity, because a normal distribution is completely defined by its first two moments (Chatfield, 2003, p. 36).

<sup>&</sup>lt;sup>5</sup> The intercept  $\beta_0$  is the expected score when the observation at the previous occasion was zero (i.e.,  $y_{t-1} = 0$ ). When the scale that is used does not include the score zero, the intercept is typically not interesting.

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*Figure 1.* Simulated time series with a positive (left) and a negative (right) autocorrelation for a valence process of a single individual. The valence process ranged from 0 to 10, with 0 indicating feeling very unhappy and 10 indicating very happy. The process was simulated for 150 time points with an intercept ( $\beta_0$ ) of 3 (left) and 6 (right; see dashed line in both graphs) and an autoregressive coefficient ( $\beta_1$ ) of 0.5 (left) and -0.5 (right), meaning that there was a positive (left) or negative (right) dependency in the data. Notice that here the intercept as such has no further meaning and is different from the mean. In the left graph, the mean ( $\mu$ ; shown by the solid black line) is 3/(1 - 0.5) = 6, indicating that on average this individual felt quite happy. In the right graph, the mean is 6/(1 + 0.5) = 4, indicating that on average this individual felt slightly unhappy.

the individual data-points, thus removing the trend from the data (Hamaker & Dolan, 2009). A drawback associated with this way of dealing with nonstationarity is that it may remove important information from the data (Molenaar et al., 1992). In the second approach, stationarity is obtained through modeling the trend with, for example, linear growth curve modeling (Tschacher & Ramseyer, 2009). Both modeling the trend as well as detrending require specifying the functional form of the trend, which can be difficult, especially when convenient parametric forms are not applicable (Adolph, Robinson, Young, & Gill-Alvarez, 2008; Faraway, 2006; Tan et al., 2012). The TV-AR model that we will present has the advantage that it can detect trends in a data-driven way, and thus no prespecifications are needed to account for a trend in the data.

Detrending or modeling the trend makes the process trend-

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stationary. However, when detrending, often only the trend due to a changing intercept is removed, and what is overlooked is that nonstationarity and trends can also occur due to changes in the autocorrelation.<sup>6</sup> For example, Figure 2 (right panel) shows a process that is nonstationary due to a change in the autocorrelation. The autoregressive function changes linearly over time, from a high value ( $\beta_1 = 0.65$ ) to a lower one ( $\beta_1 = 0.2$ ). At first, the data are characterized by a high autocorrelation, which disappears toward the end of the time series. This is evident in the figure: First there are large oscillations (a signature of a high autocorrelation), which then become smaller toward the end of the time series (indicating low autocorrelation). Removing or modeling a trend as described above will not deal with this source of nonstationarity, leaving the process covertly nonstationary. This is an important reason why TV-AR models, which can detect and model both changes in the intercept and autocorrelation simultaneously, are important.

Another reason why TV-AR models are useful is that they can test for nonstationarity. There are several tests to check for stationarity, such as the Dickey Fuller test (which can be used to test whether a unit root is present in the time series; Dickey & Fuller, 1979), and the KPSS test (which can be used to test whether the mean is stable over time, or whether it follows a linear trend; Kwiatkowski, Phillips, Schmidt, & Shin, 1992). However, there is no specific test that checks for nonstationarity due to changing autoregression or a changing mean that follows a different trajectory than a linear trend. With the TV-AR model, we present a method that can test the time invariance of the autoregressive parameter, and simultaneously check whether a trend is due to a time-varying intercept and/or a time-varying autoregressive parameter (see Figure 2). Moreover, this method allows for instantly modeling such nonstationarity.

The defining feature of a TV-AR model is that the coefficients of the model are allowed to vary over time, following an unspecified function of time (Dahlhaus, 1997; Giraitis et al., 2014). To this end, we specify

$$y_t = \beta_{0,t} + \beta_{1,t} y_{t-1} + \varepsilon_t \tag{4}$$

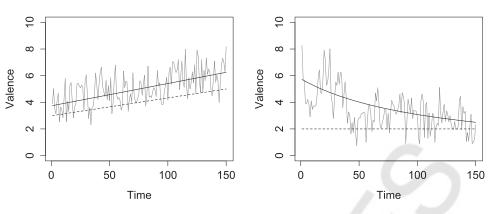
where the intercept  $\beta_{0,t}$  and the autoregressive  $\beta_{1,t}$  coefficients are now functions that can change over time.<sup>7</sup> The innovations still Fn7 form a white noise process so that the values of  $\varepsilon_t$  are independently and identically distributed, which implies that their variance is constant over time.

An important assumption of the TV-AR model is that, even though the functional form of  $\beta_{0,t}$  and  $\beta_{1,t}$  can be any function, change in the parameter values is restricted to be gradual, that is, there should be no sudden transitions. This assumption implies that the TV-AR model, as defined here, is not appropriate for time series with abrupt changes or sudden jumps. Thus, researchers should decide whether or not continuous change in parameters is plausible on the basis of the substantive knowledge of the problem at hand. If sudden, qualitative transitions are expected (e.g., as

<sup>&</sup>lt;sup>6</sup> Note that a trend can be also caused by a unit root process, such as a random walk. In this case, the process has to be differenced in order to become stationary (see, e.g., Hamilton, 1994).

<sup>&</sup>lt;sup>7</sup> Note that in Giraitis et al. (2014)  $\beta_{1,t}$  is specified as  $\beta_{1,t-1}$ . Here we use the standard notation used in Dahlhaus (1997).

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*Figure 2.* Simulated data of a valence process (with 0 indicating *feeling very unhappy* and 10 indicating *very happy*) with time-varying parameters. In the left panel, the autoregressive coefficient is time-invariant ( $\beta_1$  = 0.2), while the intercept is time-varying ( $\beta_{0,r}$ ; ranging from 3 to 5); in the right panel, the autoregressive coefficient is time-varying ( $\beta_{1,r}$ ; gradually changing from 0.65 to 0.2), while the intercept is time-invariant ( $\beta_0$  = 2). The attractor in the left panel ( $\mu_r$ ; shown by the solid black line) changes from 4 to 7, indicating that this individual felt a bit unhappy at first, but at the end of the time series felt happy, whereas the attractor in the right panel changes from circa 6 to 2.5, indicating that this individual felt happy at first, but at the end of the time series felt happy at first, but at the end felt unhappy.

would be the case in some areas of cognitive development or in mental disorders with a sudden onset) then the current methodology would not be advisable. However, if the point at which an abrupt change takes place is known, one can model the change with a TV-AR model. One could specify, for example, a TV-AR model before and after an intervention. Additionally, although a TV-AR model is designed for handling nonstationary processes, the process is still required to be *locally stationary*, meaning that  $-1 < \beta_{1t} < 1$ , for all *t* (Dahlhaus, 1997).

Assuming that the change is restricted to be gradual and the process is locally stationary, the model implied mean is (Giraitis et al., 2014):<sup>8</sup>

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$$\mu_t \approx \frac{\beta_{0,t}}{1 - \beta_{1,t}}.$$
(5)

Similarly, due to the fact that the autoregressive coefficient is allowed to vary over time, the variance of the time series is now also time-varying, that is,

$$\sigma_t^2 \approx \frac{\sigma_{\varepsilon}^2}{1 - \beta_{1,t}^2}.$$
 (6)

Note that because  $\mu_t$  can vary over time, in the literature  $\mu_t$  is often interpreted as the *attractor* (also known as baseline or equilibrium) rather than the mean of the process (Giraitis et al., 2014; Hamaker, 2012; Oravecz et al., 2011). As is the case in a time-invariant AR model, the intercept and the changing mean (attractor or trend) are distinct features of a process. The intercept typically does not have a direct psychological interpretation, whereas the attractor represents the underlying trend in the time series (see Figure 2).

# Inference of the TV-AR Model: Splines and Generalized Additive Models

In this section, we discuss how to estimate the time-varying parameters in the TV-AR model using the generalized additive model (GAM) framework. GAM models are expanded general linear models (GLMs), such that one or more terms are replaced with a nonparametric (smooth) function (Keele, 2008; Wood, 2006). This makes GAM models semiparametric models, since predictor variables (i.e., in our case  $y_{t-1}$ ) can either be modeled as in standard regression (e.g.,  $\beta_1$ ) or in a nonparametric way (e.g.,  $\beta_{1,t}$ ). We focus in this section on the nonparametric representation. Code for the figures can be found in the R-code in the Appendix under the heading IV. Inference of the TV-AR model.

The nonparametric smooth functions used here are based on regression splines. Regression splines are piecewise polynomial functions that are joined (smoothly) at breakpoints called knots (Hastie & Tibshirani, 1990). In order to clarify the concept further, we will give a simulated example (based on Wood, 2006). Specifically, data are simulated for n = 20 time points according to a sine wave:  $y_t = \sin(\frac{2\pi t}{20}) + \epsilon_t$ , where  $\epsilon_t \sim N(0, 0.3^2)$ . We denote the time points in the data as  $t_i$  with  $i = 1, \ldots 20$ . The data are represented as the small black dots in the first and last panel of Figure 3. To fit these data, we start with a simplified TV-AR F3 model

$$y_t = \beta_{0,t} + \varepsilon_t \tag{7}$$

with only a time-varying intercept and no autoregressive parameter.

<sup>8</sup> To derive a model-implied mean of the TV-AR, we can write:

$$\mu_{t} = E[\beta_{0,t} + \beta_{1,t}y_{t-1} + \varepsilon_{t}]$$

$$= E[\beta_{0,t}] + E[\beta_{1,t}y_{t-1}] + E[\varepsilon_{t}]$$

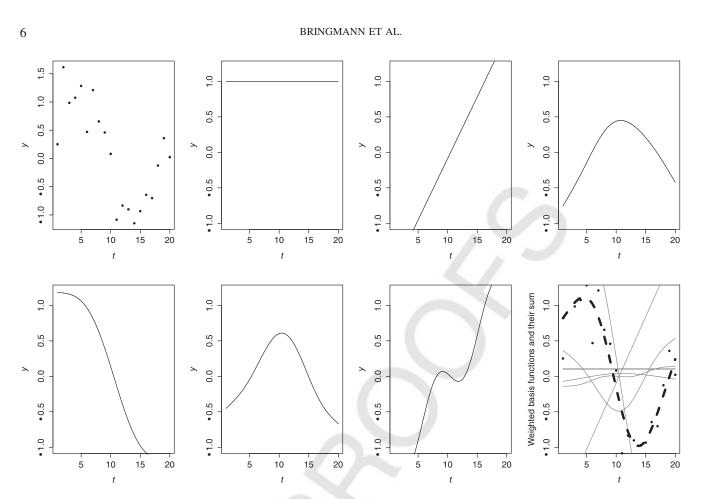
$$= \beta_{0,t} + \beta_{1,t}\mu_{t-1}$$

$$\approx \beta_{0,t} + \beta_{1,t}\mu_{t} \qquad (14)$$

where the latter approximation results from the fact that, in contrast to a standard AR model where we have  $E[y_t] = E[y_{t-1}] = \mu$ , the expectations of  $y_t$  and  $y_{t-1}$  are not exactly equal for a TV-AR model. However, because the parameters  $\beta_{0,t}$  and  $\beta_{1,t}$  are only allowed to change gradually, we can assume that  $\mu_{t-1}$  is reasonably well approximated by  $\mu_t$ , so that we have Equation 5. The derivation of the time-varying variance is similar to the derivation of the time-varying mean.

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*Figure 3.* The six basis functions for the curve  $\beta_{0,t}$  using a cubic regression spline basis. Just as in standard regression, all basis functions  $R_i(t)$  are weighed by multiplying them with their corresponding  $\alpha_i$  coefficients. The contribution of each basis function to the solution is estimated using penalized regression and the  $\hat{\beta}_{0,t}$  (the thick black dashed line in the bottom right panel) is a weighted sum.

The goal is to find the function  $\beta_{0,t}$  that tracks the general relation between *y* and *t* (which for this example is the sine wave underlying the data) as well as possible. In order to find the optimal smooth function estimating  $\beta_{0,t}$ , the following penalized least squares loss function is minimized:

$$\sum_{i=1}^{n} [y_i - \beta_{0,t_i}]^2 + \lambda \int_{-\infty}^{+\infty} [\beta_{0,t}^{"}]^2 dt.$$
(8)

In the first part of Equation 8 one can recognize the ordinary least squares minimization  $\sum_{i=1}^{n} [y_i - \beta_{0,i_i}]^2$ , which measures the distance between the function and data points. The last part is the roughness penalty  $\lambda \int_{-\infty}^{+\infty} [\beta_{0,i}^{"}]^2 dt$ . This is an integrated squared second derivative that defines wiggliness, because the second derivative is a measure of curvature of the function whereas the integral sums up this measure along the entire domain of the function (Keele, 2008). Note that the square is needed to treat negative and positive curvature identically. The  $\lambda$  is a tuning parameter that controls the smoothness of the function. Small values of  $\lambda$  practically eliminate the penalty, thereby not penalizing for wiggliness and opening the possibility for wiggly functions. Large values of  $\lambda$  give a lot of weight to the penalty, thereby penalizing for wiggliness and restricting the possibility for wiggly functions. Minimizing the whole function leads to an optimal trade-off between goodness of fit and smoothness.<sup>9</sup>

The solution to the problem in Equation 8, denoted  $\hat{\beta}_{0,t}$ , can be expressed as a finite weighted sum of a set of predefined functions, known as basis functions. This can be written as follows:

$$\hat{\beta}_{0,t} = \hat{\alpha}_1 R_1(t) + \hat{\alpha}_2 R_2(t) + \hat{\alpha}_3 R_3(t) + \dots + \hat{\alpha}_K R_K(t), \qquad (9)$$

where we have expressed the solution in terms of *K* basis functions  $R_1(t), \ldots, R_K(t)$  and *t* represents the predictor variable (time, in our case). The basis functions can be evaluated at every time  $t_i$  in the data and therefore the values  $R_1(t_i), \ldots, R_K(t_i)$  can be collected in a  $n \times K$  design matrix *X* so that the optimal regression weights can be determined by linear regression methods (see below).

Various options exist for choosing the smoothing basis, that is, the set of basis functions  $R_1$  to  $R_K$ . Commonly used smoothing bases are *cubic regression splines* and *thin plate regression splines* (the latter being the default setting in the package *mgcv*), which represent alternative strategies with different properties of how the

<sup>&</sup>lt;sup>9</sup> Note that the least squares criterion can be used here because we assume continuous normally distributed data. In the more general case, the least squares criterion is replaced by minus the likelihood.

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basis functions are chosen (Wood, 2006). Cubic regression splines are segmented cubic polynomials joined at the knots, and are constrained to be continuous at the knot points as well as to have a continuous first and second derivative (Wood, 2006). With cubic regression splines the locations of knots have to be chosen, the default setting in the *mgcv* package being that the knot points are automatically placed (equally spaced) over the entire range of data.

In contrast, the thin plate regression splines approach automatically starts with one knot per observation and then uses an eigen-decomposition to find the basis coefficients that maximally account for the variances in the data. Thus, thin plate regression splines circumvent the choice of knot locations, reducing subjectivity brought into the model fit (Wood, 2006). Furthermore, unlike cubic regression splines, thin plate regression splines can handle smoothing in high-dimensional problems (e.g., when multiple independent variables occur). However, in one-dimensional problems, such as the one considered here, cubic and thin plate regression splines will lead to very similar solutions.

For our example, we have chosen a thin plate regression spline smoothing basis with K = 6 basis functions. The six basis functions are plotted in the panels 2-7 of Figure 3. The first two basis function are defined as  $R_1(t) = 1$  and  $R_2(t) = t$ . Here one can recognize the constant and the first predictor variable of a standard linear regression model. The other four basis functions  $(R_3 - R_6)$ have a more complicated shape (for examples of such functions, see Gu, 2002; Keele, 2008; Wood, 2006). Additionally, in thin plate regression every basis function that is added is wigglier than the previous basis function. For example, basis function  $R_6$  is wigglier than  $R_5$ . Note that in contrast to cubic splines, where the basis functions depend on the knot location, in thin plate splines a basis function cannot be associated with a knot location. Furthermore, the basis functions are evaluated at every value of t (also with the cubic spline smoothing basis). This is important to point out, as regression splines are defined as segmented polynomials that are joined at the knot points, so evaluations of the basis functions may prima facie seem to be restricted to particular segments.

After choosing the smoothing basis and the number of basis functions, estimating the time-varying function  $\beta_{0,t}$  simply boils down to the estimation of the weights (denoted as  $\alpha_i$  above) of the linear combination in a penalized regression sense (see below). In Figure 3, the final panel shows the weighted basis functions as well as the sine wave that is the final smooth function (i.e.,  $\hat{\beta}_{0,t}$ , the thick dashed line).

Using a regression spline based method to estimate a smooth function raises the question of how many basis functions are needed to get a good fit. The usual approach is to place more basis functions than can reasonably be expected to be necessary, after which the function's smoothness is controlled by the roughness or wiggliness penalty as described earlier  $(\lambda \int_{-\infty}^{+\infty} [\beta_{0,i}]^2 dt$ ; see Wood, 2006). An attractive feature of spline regression methods is that the penalized loss function eventually boils down to a relatively simple penalized regression problem (see Wood, 2006). Thus, one can choose a reasonably large number of basis functions (so that in principle even very wiggly functions can be handled by the model), but then too wiggly components of the basis functions that are unnecessary are downplayed based on the value of the penalization tuning parameter  $\lambda$ . For instance, in our example the

wiggliest basis function  $R_6$  (panel 7 in Figure 3) is clearly penalized, as it appears as an almost flat horizontal line in the last panel of Figure 3.

Of course, the next question is then: What is a good value for the penalty parameter  $\lambda$ ? If the value of  $\lambda$  is too small, the estimated function is not smooth enough, but if  $\lambda$  is set too high, the function may oversmooth the data. Commonly, the optimal value of  $\lambda$  is determined using the generalized cross-validation method (GCV; Golub, Heath, & Wahba, 1979). The idea of (ordinary) crossvalidation is that first a model, in this case a regression spline with a certain value of  $\lambda$ , is fitted on part of the data, for example leaving one datum out. In a second step, it is measured how well the estimated model can predict the other part of the data, for example the datum that was left out. However, with splines this process is computationally intensive and sensitive to transformations of the data (Wood, 2006). Therefore, the generalized crossvalidation score is used instead, which follows the same principle, but is invariant to transformations (Keele, 2008). The lowest GCV score indicates the optimal  $\lambda$  value and thus optimal smoothness of the estimated smooth function.

All of the above steps are implemented in the mgcv package in *R* (Wood, 2006). Using this software, one only has to define sufficiently many basis functions. The default for all splines is 10 basis functions. For the current example, detecting the relation between *y* and *t*, the command in *R* would be  $gam(y \sim s(t, bs='tp', k=6))$ , where the function *s* indicates the use of a smooth function for its argument (the predictor t in this case), bs indicates which smoothing basis is used (thin plate in this case), and k indicates the number of basis functions (see also the R-code in the Appendix). In addition to the GCV score and the estimated smooth function, the mgcvpackage also provides (a) *p* values; (b) a measure of nonlinearity (eff and ref.*df*); (c) 95% confidence intervals (CIs); and (d) model fit indices, all of which we elaborate on below.

- 1. The *p* values for the smooth function result from a test of the null hypothesis that the smooth time-varying function is actually zero over the whole time range (Wood, 2013).
- 2. As nonparametric smooth functions (such as  $\beta_{0,t}$ ) are difficult to represent in a formulaic way, a graphical representation is usually needed to get insight into the form of the function (see for instance Figure 3; Faraway, 2006). However, besides a plot of the smooth function, the mgcv package also provides a measure of nonlinearity in the form of the effective degrees of freedom (edf). AQ:2 Basically, the edf refers to the number of parameters needed to represent the smooth functions. At first sight, one may think that this is equal to the number of basis functions, but because of the penalization that is not the case. The reason why the penalization decreases the effective degrees of freedom is that the parameters are not free to vary because of the penalizations (Wood, 2006). The higher the edf, the more wiggly the estimated smooth function is, and an edf of 1 indicates a linear effect (Shadish, Zuur, & Sullivan, 2014). Furthermore, the edf also gives an indication of how much penalization took place and thus may serve as a diagnostic: The closer the edf is to the number of basis functions, the lower the

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#### 8

F4

penalization. Usually, an edf close to the number of basis functions means that additional basis functions should be added to capture the shape of the function. The ref.*df* is the reference degree of freedom used for hypothesis testing (Wood, 2013).

- The 95% confidence intervals (CIs) around the smooth curve reflect the uncertainty of the smooth function. As the confidence intervals are obtained through a Bayesian approach, they are strictly speaking credible intervals, or Bayesian confidence intervals as referred to by Wood (see Wood, 2006).
- 4. Finally, model selection criteria can be retrieved with the package (such as BIC and AIC), where the lowest fit indices indicate the best model fit. When using the BIC and AIC for penalized models, note that the degrees of freedom are determined by the edf number and not by the number of parameters (see for more information Hastie & Tibshirani, 1990).

We have assumed a simple model with only a time-varying intercept to explain the fundamentals of splines. For the more realistic general TV-AR model, the time-varying autoregressive function is estimated in a similar way (see for further information Wood, 2006).

# Guidelines Regarding the TV-AR Model: A Simulation Study

To evaluate how the TV-AR model performs under different circumstances using the default settings, we carried out a simulation study. In addition, we investigated the robustness of our method against violations of the assumption of gradual change, by considering also functions that change nongradually. Here, we will give a general overview of the simulation conditions. In the supplementary material the simulation setup is described in detail. In addition, there is *R-code* in the Appendix exemplifying some of the simulation results under the heading V. Guidelines TV-AR Model.

In the simulation study, we varied three factors: the generating function, low or high values for the model parameters, and the sample size. First, we had five generating functions for the intercept  $\beta_{0,r}$  and the autoregressive parameter  $\beta_{1,r}$ : (a) both are invariant over time, (b) both increase linearly over time, (c) both follow a cosine function over time, (d) both follow a random walk, and (d) both follow a stepwise function (see also Figure 4). Note that the random walk and the stepwise function are nongradually changing functions. Strictly, the TV-AR model is thus not expected to recover these functions. Instead, we consider these functions to investigate the robustness of TV-AR in nongradual conditions. The second factor we varied was the maximum absolute values of the parameters (low or high maximum value). The third factor was sample size (30, 60, 100, 200, 400, 1,000).

Estimation was executed using five models: (a) a TV-AR model using the default settings (a thin plate regression spline basis using 10 basis functions); (b) a TV-AR model with only a time-varying intercept and a time-invariant autoregressive parameter using the default settings; (c) a TV-AR model with only a time-varying autoregressive parameter using the default settings; (d) a standard time-invariant AR model; and E) a thin plate regression spline basis using 30 basis functions.

We evaluated the estimates of all models with mean squared errors (*MSE*) and coverage probabilities (CP; see the Appendix for a detailed explanation of these measures). Furthermore, we analyzed how well the BIC, AIC, and GCV could distinguish between time-varying and time-invariant processes. Last, we looked at the significance of the parameters and the effective degrees of freedom (edf) if applicable.

#### **Results and Guidelines**

The results show that the time-varying AR model was able to estimate all gradually changing generating functions (invariant, linear, cosine) very well using the default settings of the mgcv package in R (i.e., using 10 basis functions and thin plate regression splines; see Figures 4 and 5). Around 200 time points were F5 needed for detecting a small change, such as a small linear increase over time, but large changes could already be detected with 60 time points.

In general, none of the model selection methods (BIC, AIC, and GCV) performed well in selecting the correct model out of Models A, B, C, and D (e.g., with 100 time points in the high condition of the linear increase, the BIC selects the correct model (Model A) in only 60% of the cases). However, the BIC does relatively well in distinguishing between the time-invariant Model D and the time-varying models (the three variants A, B, and C combined). For example, with 100 time points in the high condition of the linear increase, the BIC selects the correct class (invariant vs. time-varying) in circa 97% of the cases.<sup>10</sup>

As the BIC cannot be used for selecting the exact time-varying model (Model A, B, or C), additional criteria are needed. One possibility is to fit a TV-AR model and check the significance of the parameters (intercept and autoregressive parameter). If the intercept is significant, one can be confident that the intercept is time-varying, especially with at least circa 100 time points. This is because the TV-AR model automatically includes an (standard time-invariant) intercept, and significance implies that another, time-varying, intercept is needed. In contrast, in the case of the autoregressive parameter, significance entails that the parameter is valuable for the model, and thus should be kept, but it does not give information about whether it is a time-varying parameter or not. Additionally, a high edf is an indication that the parameter is time-varying, but note that the edf cannot be used to discriminate between time-invariant parameters and linearly increasing time-varying parameters, as they will often both have an edf of circa 2.

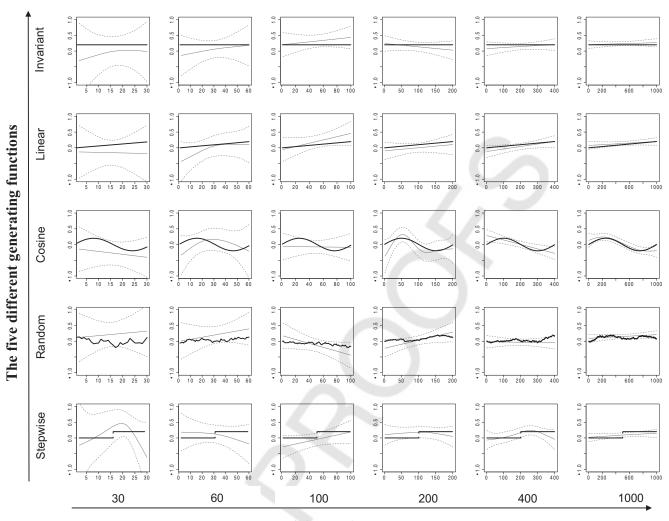
Even when the assumption of gradual change was violated, the TV-AR model was still able to estimate the general pattern of change (i.e., the trend-like fluctuations in the random walk), but not abrupt changes (such as in the stepwise function) or fast changes (i.e., the small-magnitude fluctuations in the random walk

Fn10

<sup>&</sup>lt;sup>10</sup> Note that the AIC and GCV were not as accurate as the BIC. For example, with 100 time points in the high condition of the linear increase, the AIC and GCV selected the correct class (invariant vs. time-varying) in only 73% and 76% of the cases, respectively.

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Number of time points

*Figure 4.* Graphical representations of the generating functions of the autoregressive parameter for the low condition. The different true underlying functions  $\beta_{1,t}$  are represented as thick black solid lines and the estimated  $\hat{\beta}_{1,t}$  as gray solid lines, the gray dashed lines being the 95% CIs. The estimations are based on the median of the *MSE* values of the 1,000 replications.

process). An exception was the condition with 1,000 time points of the stepwise function, where the large jump could be detected quite well (see Figure 5). To get satisfying estimations in these cases, more time points are needed, and the amount of basis functions should be large enough. In general, it is advisable to always check whether you have enough basis functions. A good indication that you do not have enough basis functions and should increase their number is that the effective degrees of freedom (edf) come close to the number of basis functions (Wood, 2006). The simulation study showed that the average coverage probabilities of especially the nongradually changing functions are clearly improved by increasing the number of basis functions (in this case from 10 to 30 basis functions; see Table 1). This lines up well with the advice given in general to have a high enough number of basis functions to allow for enough wiggliness in the estimated function (Wood, 2006).

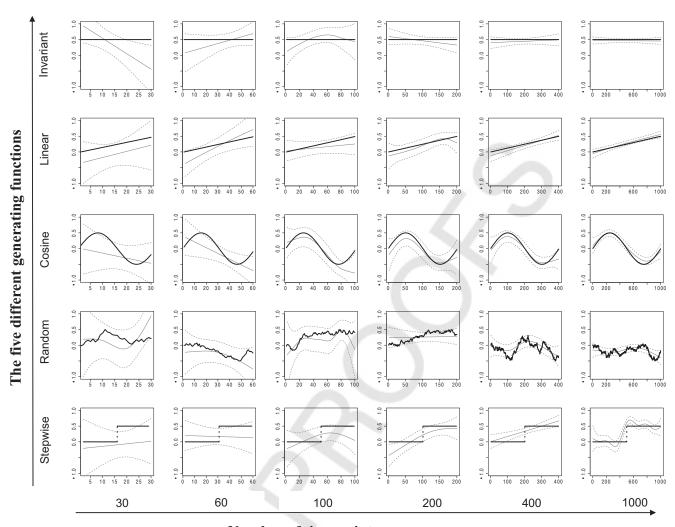
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#### An Empirical Example

We applied the TV-AR model to data of two individuals who took part in a long isolation study, the MARS500 project, in which psychological and physiological data have been collected to study the effects of living in an enclosed environment for the duration of a real potential mission to Mars (i.e., 520 days; for more information see http://www.esa.int/Mars500). We focus here on emotional inertia, which is studied in the context of affective research. Emotional inertia is defined as the temporal dependency of individual emotions, or the self-predictability of emotions, and is typically modeled with an AR model (Kuppens et al., 2010; Suls, Green, & Hillis, 1998). However, a study by Koval and Kuppens (2012) showed that emotional inertia is not a trait-like characteristic, but is itself prone to change, causing the data to be nonstationary (see also de Haan-Rietdijk et al., 2014; Koval et al., in

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Number of time points

*Figure 5.* Graphical representations of the generating functions of the autoregressive parameter for the high condition. The different true underlying functions  $\beta_{1,t}$  are represented as thick black solid lines and the estimated  $\hat{\beta}_{1,t}$  as gray solid lines, the gray dashed lines being the 95% CIs. The estimations are based on the median of the *MSE* values of the 1,000 replications.

press). They showed, among other things, that individuals who anticipated a social stressor had a significant decrease in their emotional inertia, which means that to model the process of inertia correctly, the autoregressive parameter should be allowed to vary over time. In the MARS500 example, being isolated can be seen as a social stressor. Furthermore, it is plausible that the longer one is isolated, the more social stress there is. To study if and how inertia changed due to social isolation, we analyzed time series data from two persons involved in the MARS500 study using the TV-AR model.

# Method

#### **Data Description**

The MARS500 study consisted of six healthy male participants (average age was 34 years), who all signed a written informed consent before participating in this experiment. In accordance with

the Declaration of Helsinki, the protocol was approved by The Ethics Committee of the University Hospital Gasthuisberg of Leuven (Belgium) and the ESA Medical Board before the research was conducted. We focus here on the dynamics of the variable "valence" of two participants. Each morning, the participants indicated on a  $21 \times 21$  grid how they were feeling at that moment. The horizontal axis of the grid referred to valence and the vertical axis to arousal. Only the valence score (on 21-point scale) will be analyzed here. A high score indicates experience of highly positive feelings, and a low score experience of highly negative feelings.<sup>11</sup> Fn11

<sup>&</sup>lt;sup>11</sup> Although the measurement was done on a daily basis, on some days there were multiple measures, which was due to extra physiological tests that required additional measurements of valence and arousal. In these cases, we only used the first measure of the day.

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N	True underlying function									
	Invariant		Linear		Cosine		Random		Step	
	Low	High	Low	High	Low	High	Low	High	Low	High
30	86	67	89	83	89	83	92	87	89	78
60	92	84	93	91	91	84	94	88	91	83
100	93	90	93	91	92	85	93	86	92	83
200	95	92	95	94	89	92	92	84	90	79
400	95	93	95	94	87	94	91	81	86	80
1,000	95	95	95	95	89	96	86	78	82	82
1,000 K = 30	95	94	94	95	91	96	87	83	84	87

Coverage Probabilities (CP) of the Autoregressive Function in % Using Thin Plate Regression Splines

*Note.* Here the average CP of every simulation condition is given. Low and high stand for low and high value conditions for the maximum absolute values of the time-varying parameters. Note that the last line in the table uses the same settings as the previous line, except now 30 instead of 10 basis functions (K) are used.

There was 29% and 18% missingness in the data of Participant 1 **F6**, **Fn12**and 2, respectively (see Figure 6 for the raw data).<sup>12</sup>

#### Analyses

We consider the following four models.

Table 1

**Model 1.** In Model 1, both the intercept and the autoregressive parameter are allowed to vary over time. The time-varying autoregressive parameter implies that the temporal dependency or emotional inertia (i.e., how self-predictable the emotion is) changes over time. Since the mean (or the attractor of the process) is a function of the intercept and the autoregressive parameter, it most likely also changes over time in this model:<sup>13</sup>

$$Valence_{t} = \beta_{0,t} + \beta_{1,t} Valence_{t-1} + \varepsilon_{t}.$$
 (10)

**Model 2.** In Model 2, the intercept is allowed to fluctuate over time, but the autoregressive parameter is fixed over time, meaning that the temporal dependency (or emotional inertia) is time-invariant. Due to the changing intercept, the person's attractor also changes over time:

$$Valence_{t} = \beta_{0,t} + \beta_{1} Valence_{t-1} + \varepsilon_{t}.$$
 (11)

**Model 3.** In Model 3, the intercept is fixed over time, while the autoregressive parameter is allowed to vary over time. As indicated in the description of Model 1, a time-varying autoregressive parameter means that the temporal dependency (or emotional inertia) of the process changes over time. However, fixing the intercept implies that the attractor changes over time, but this is fully accounted for by changes in the temporal dependency (i.e., the autoregressive parameter):

$$Valence_{t} = \beta_{0} + \beta_{1,t} Valence_{t-1} + \varepsilon_{t}.$$
 (12)

**Model 4.** Finally, Model 4 is the standard AR(1) model, in which both the intercept and the autoregressive parameter are time-invariant; as a result the mean (i.e., a time-invariant attractor) is also fixed over time. This means that the temporal dependency (or emotional inertia) is completely constant over time, that is, both the temporal dependency (or emotional inertia) and the attractor value of the process remain the same over time:

$$Valence_{t} = \beta_{0} + \beta_{1} Valence_{t-1} + \varepsilon_{t}.$$
 (13)

Following the guidelines presented in the previous section, we first checked if the process was time-varying or not. For this purpose, we used the BIC: If the BIC selects Model 1, 2, or 3 the process is probably changing over time, and otherwise (i.e., if Model 4 is selected) the process is probably time-invariant. In the latter case, a standard AR model should be used; otherwise a TV-AR model is appropriate. Second, to check which parameters are time-varying, we considered whether the smooth parameters were significantly different from zero and thus were needed in the model. As noted before, a significant intercept indicates that this parameter is time-varying, whereas a significant autoregressive parameter does not entail that it is time-varying. Therefore, in a third step, when the autoregressive parameter was significant we checked if the edf was higher than 1. Additionally, we checked whether the residuals (estimated innovations  $\hat{\varepsilon}_t$ ) indicated autocorrelation over time, satisfied the equal variance assumption and were normally distributed.

The analyses reported here were based on the default settings, that is, a thin plate regression spline basis with 10 basis functions (i.e., K = 10). We also ran all of the analyses with a cubic regression spline basis and thin plate regression splines with 30 basis functions (i.e., K = 30), but all results were highly similar and led to the same conclusions.

#### Results

As can be seen in Figure 6 (left panel), in the data of Participant 1, a clear trend is apparent, whereas the data for Participant 2 do not contain any clear time trend (Figure 6 right panel). For both

<sup>&</sup>lt;sup>12</sup> Note that the TV-AR model can also be used with missing data, although the more missingness the less power one has to detect the underlying process. Additionally, one has to assume that the missingness is (completely) at random.

<sup>&</sup>lt;sup>13</sup> Of course it is possible, though unlikely, that the changes in the autoregressive parameter are exactly countered by the changes in the intercept (see Equation 5). In this case, the attractor would be time-invariant, while the temporal dependency would fluctuate over time.

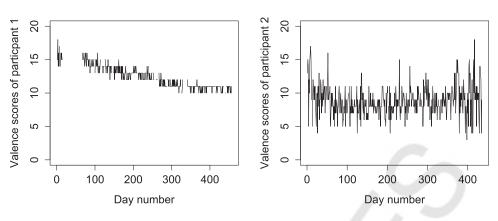


Figure 6. The raw data of the variable valence for Participant 1 (left) and Participant 2 (right).

participants the assumptions held for the selected models: The residuals for both participants did not indicate any autocorrelation over time, did not violate the equal variance assumption and were normally distributed.

For Participant 1, the BIC indicated that the underlying process

T2

F7

was varying over time and thus nonstationary (Model 2 was selected as the best model, although the differences between Model 1 and 2 were fairly small, see Table 2). Consequently, fitting the TV-AR model showed that the function of the intercept was significantly different from zero (F = 3.42, p = .0046, edf = 4.50, ref.df = 5.20), while the function of the autoregressive parameter was not (F = 0.87, p = .51, edf = 5.01, ref.df = 5.62). Thus, only a time-varying intercept was needed in the TV-AR

model. Based on visually inspecting Figure 7, the function of the intercept process (upper panel) is clearly varying over time, whereas the CIs of the function of the autoregressive parameter (middle panel) always include zero (the zero is represented by the dashed gray line) and the function does not clearly go up or down at any point in time. Taking all of these considerations into account, Model 2, with a time-varying intercept and a time-invariant autoregressive parameter of zero, seems to be the best fitting model.

For Participant 2, the BIC indicated that Model 3 had the best model fit and thus a TV-AR model was estimated. In line with this result, Model 1 (Equation 10) implied that the function of the autoregressive parameter was significant and should be kept in the model (F = 8.32, p < .0001, edf = 5.17, ref.df = 6.15), while the function of the intercept was not significant and thus time-invariant (F = 0.15, p = .70, edf = 1.00, ref.df = 1.00). Although significance does not imply that the autoregressive parameter is time-varying, the edf was clearly higher than 1. In addition, visual

 Table 2

 Model Selection for Participants 1 and 2 Using the BIC Indices

Model	BIC Participant 1	BIC Participant 2			
Model 1	688	1,896			
Model 2	684	1, 894			
Model 3	696	1, 890			
Model 4	868	1, 899			

Note. Lowest fit indices are in bold.

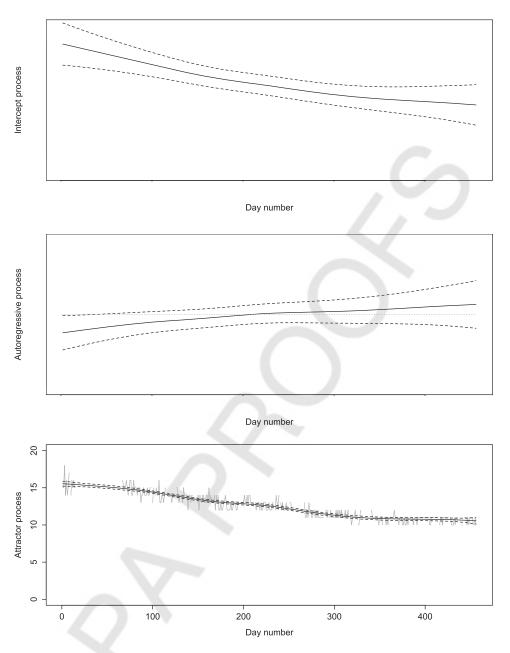
inspection of Figure 8 also clearly indicates that the autoregressive F8 function (middle panel) of Participant 2 changes over time. Thus, Model 3, with a time-invariant intercept and a time-varying autoregressive parameter, seems to be the best model.

In sum, in the data for Participant 1, no inertia or autocorrelation of valence in the data is apparent, but rather it is the intercept that changes (see Figure 7, panel 3). In this specific case, the attractor is equal to the intercept as the autoregressive parameter equals zero. Participant 1 simply feels less happy as the isolation experiment proceeds, as represented by the changing intercept and attractor. This is not necessarily in contradiction with the results found by Koval and Kuppens (2012) as we do not know how much emotional inertia Participant 1 had before the isolation experiment. It is possible, for example, that this participant had some level of emotional inertia before going into isolation, but as soon as the experiment started, his emotional inertia decreased to zero, which would be in line with the previous findings of Koval and Kuppens (2012). In contrast, Participant 2 starts the isolation experiment relatively happy and with a high spill-over of valence (high inertia), but already after a few days, his inertia decreases until it gets to zero around 100 days, and also his valence becomes more negative (see the attractor in the last panel of Figure 8). Toward the end of the experiment, there is again a light increase in his feeling of happiness and his inertia. This result is in line with research of Koval and colleagues, which suggests that as stress increases (the longer one is isolated) inertia decreases, and thus affect becomes less predictable (Koval & Kuppens, 2012).

Note that if one had ignored this nonstationarity in the data, a standard autoregressive model (thus, *Model 4*) would have led to inaccurate conclusions about these two participants. For Participant 1, ignoring nonstationarity would have led to inferring a highly significant autoregressive coefficient ( $\beta_1 = 0.85$ , t(325) = 27.43, p < .0001), that is, an extremely high inertia or a high predictability of his valence. For Participant 2, ignoring nonstationarity would have led to the conclusion that there was a positive inertia ( $\beta_1 = 0.20$ , t(420) = 4.29, p < .0001), and the fact that his inertia was actually varying over time would have gone unnoticed.

In general, even though inertia is already well known to vary in strength greatly across individuals, it is still often studied as a trait of an individual. With the TV-AR model we can study inertia throughout the whole study period, creating an inertia value for

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*Figure 7.* Estimation results for the TV-AR model for Participant 1. Every panel represents a different parameter of the TV-AR model: the upper panel the intercept, the middle the autoregressive and the lowest the attractor. Note that the attractor process is plotted over the actual valence scores (represented in gray).

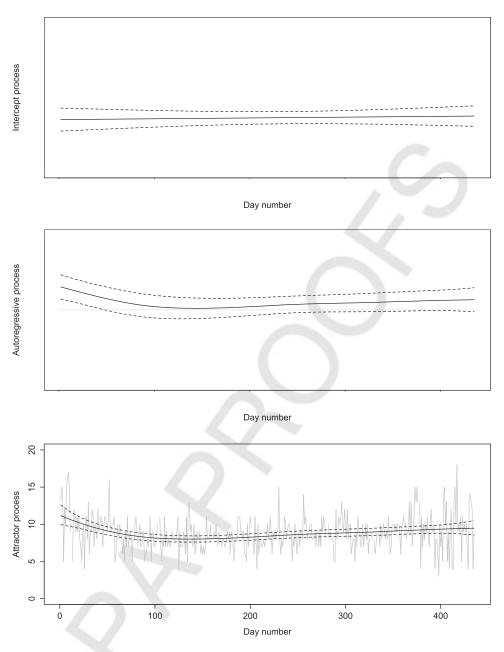
every single time point. In future studies, it would be fruitful to take into account that inertia can change over time, even from day to day or faster, and of course, also in other contexts than social stress.

Furthermore, these two applications show how important it is in general to use a TV-AR model, as different conclusions would have been drawn with a standard AR model. In addition, with the TV-AR model trends as well as (time-varying) autoregressive parameters can be detected in one step: Even though the first example above (Participant 1) involves a trend-stationary process and prespecifying the exact (nonlinear as the edf of 4.50 indicates) trend would have led to the same conclusions, this would have been much more difficult than with the TV-AR model. Psychological data can be nonstationary for various reasons, and the TV-AR model offers a simple exploratory tool for detecting such changing dynamic processes.

#### Discussion

In this article, we have introduced a new way to study changing dynamics: the semiparametric TV-AR model. This model fills a gap in the literature, because most standard autoregressive models

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*Figure 8.* Estimation results for the TV-AR model for Participant 2. Every panel represents a different parameter of the TV-AR model: the upper panel the intercept, the middle the autoregressive, and the lowest the attractor. Note that the attractor process is plotted over the actual valence scores (represented in gray).

do not take into account nonstationarity, even though many psychological processes are likely to be nonstationary. Therefore, there is a need for an easily applicable method for studying such nonstationarity or changing dynamics. The semiparametric TV-AR model presented in this article is exactly such a tool.

As shown by the simulations and application in this article, the TV-AR model can estimate nonstationary processes well and has significant potential for studying changing dynamics in psychology. For example, the TV-AR model can help to detect and specify different kinds of nonstationarity in the data. Currently, it is common practice to focus on the trend that is apparent in the data,

and to transform the time series so that it becomes trend stationary. However, even if the trend could be perfectly specified, which is often difficult, nonstationarity may not be fully accounted for, because the autocorrelation structure of the data can also change over time. Furthermore, a changing autocorrelation is not easy to detect visually, nor is there a test to detect such nonstationarity. With the semiparametric TV-AR model, all such problems can be dealt with in one single step: Trends in the data and changes in the autoregressive process can be detected at once, and even more importantly, no prespecifications are necessary, as has been shown in the real data application.

#### CHANGING DYNAMICS

It is therefore clear that the semiparametric TV-AR model is important in the case of nonstationary data. However, its potential range of application is much broader. As little is known about how and when psychological dynamics change, we would recommend to always run a TV-AR model next to a standard AR model as part of regular analysis if enough time points (circa 100) are available. In this way, the model can be used as a diagnostic tool for probing whether there is nonstationarity in the time series, and for detecting and specifying changing dynamics, such as the trend. For example, if the time series turns out to have a trend that is linear instead of nonparametric, a simpler parametric model can be specified based on the TV-AR analyses.

We have considered the simplest form of a TV-AR model, and will now elaborate on some of the extensions that are possible. We studied temporal dependency with a lag order 1 TV-AR model, but one can imagine that the temporal dependency is not only apparent between the two closest occasions, but also between occasions further apart, in which case a TV-AR model with lag order 2 or larger is necessary. Such extra lags can be easily added into a TV-AR model in the same manner as they are added into standard AR models through the inclusion of more lagged predictors.

Another sensible extension involves generalization of the model to multivariate data. The TV-AR model is currently only applicable to the univariate case, while it is often more realistic that a variable is not only predicted by itself, but also by other variables, which evokes the need to analyze psychological dynamics as a multivariate system. Such an extension would lead to a time varying vector AR (TV-VAR) model, and comes with new challenges, as both auto-correlations and cross-correlations would have to be modeled in this case. Yet another natural, but even more challenging, extension would be a TV-AR multilevel extension based on current multilevel (V)AR models (Bringmann et al., 2013; de Haan-Rietdijk et al., 2014; Jongerling, Laurenceau, & Hamaker, 2015). To the best of our knowledge, this is currently not possible, as the mgcv software cannot be used to estimate a flexible smooth function for the population (i.e., the population average) and to allow for flexible interindividual variation for that smooth function. An additional extension could be time-varying error variance, so that also the time-varying variance of a process could be fully accounted for. However, with current software, only the intercept and the autoregressive parameter (and not the error variance) can be modeled as time-varying parameters. Further research should also consider the combination of gradual and abrupt changes, so that when the point of an abrupt change is known, it could be easily adjusted in the TV-AR model.

Even though the TV-AR model is easily applicable, the number of time points needed is a potential limitation. While 100 time points per participant would be preferable, currently most longitudinal studies in psychology gather around 60 time points or less (aan het Rot et al., 2012). Another limitation of the TV-AR is the assumption of gradual change. Although we have shown in the simulation study that with many time points and a large abrupt change the TV-AR model is quite robust and still gives an indication of the sudden jump, other models are probably more suitable for studying sudden change. Such models include the threshold autoregressive model (TAR; e.g., Hamaker, 2009; Hamaker, Grasman, & Kamphuis, 2010), its multilevel extension, multilevel TAR (de Haan-Rietdijk et al., 2014), or the regime-switching state-space model (cf. Hamaker & Grasman, 2012; Kim & Nelson, 1999).

Furthermore, as the semiparametric TV-AR model is an exploratory tool, the standard errors of the time-varying parameters are likely to be less satisfactory compared with confirmatory, raw-data maximum likelihood approaches, such as the state-space approach. Additionally, estimating a TV-AR model in a state-space modeling framework has the advantage that measurement error can be taken into account, which is not possible with the semiparametric TV-AR model (Schuurman, Houtveen, & Hamaker, 2015). Thus, future research should aim at comparing the exploratory semiparametric TV-AR model with confirmatory approaches.

In sum, the semiparametric TV-AR model presented here is an easy to use tool for detecting and modeling nonstationarity. Many extensions are possible, and future research is needed to uncover all the possibilities and limitations of this innovative framework. By introducing the model and explaining its application in standard software, we hope to have made it available to a broad range of psychologists studying human dynamics.

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Received March 20, 2015 Revision received February 8, 2016

Accepted February 24, 2016 ■

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